

Efficient Object Search in Game Maps

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Abstract

1 Video games feature a dynamic environment where
2 locations of objects (e.g., characters, equipment,
3 weapons, vehicles etc.) frequently change within
4 the game world. Although searching for relevant
5 nearby objects in such a dynamic setting is a fun-
6 damental operation, this problem has received lit-
7 tle research attention. In this paper, we propose a
8 simple lightweight index, called Grid Tree, to store
9 objects and their associated textual data. Our in-
10 dex can be efficiently updated with the underly-
11 ing updates such as object movements, and sup-
12 ports a variety of object search queries, including
13 k nearest neighbors (returning the k closest ob-
14 jects), keyword k nearest neighbors (returning the
15 k closest objects that satisfy query keywords), and
16 several other variants. Our extensive experimen-
17 tal study, conducted on standard game maps bench-
18 marks and real-world keywords, demonstrates that
19 our approach has up to 2 orders of magnitude faster
20 update times for moving objects compared to state-
21 of-the-art approaches such as navigation mesh and
22 IR-tree. At the same time, query performance of
23 our approach is similar to or better than that of IR-
24 tree and up to two orders of magnitude faster than
25 the other competitor.

1 Introduction

27 Video games offer a virtual environment in which players in-
28 teract with a variety of objects such as game characters, units,
29 vehicles, equipment, weapons and other types of items. These
30 objects can be moving, changing, appearing or disappearing,
31 creating a dynamic and ever-evolving game world. This dy-
32 namic nature of games poses a unique challenge for efficient
33 object search – searching for relevant nearby objects – in the
34 game world. Object search is a crucial operation in video
35 games, enabling players to navigate the game world, inter-
36 act with objects, and complete tasks. It is also used by game
37 engines in various contexts, including game AI, physics sim-
38 ulation, scripting, inventory management, quest tracking, and
39 object tracking. For instance, the game AI employs object
40 search to locate nearby enemies, allies, weapons, and other
41 objects relevant to their locations and actions.

While finding shortest path/distance between two points in
a game map, which is represented as a Euclidean plane con-
taining polygonal obstacles, has been very well studied [Yap
et al., 2011; Shen *et al.*, 2020; Nash *et al.*, 2007], object
search has received little research attention despite its practi-
cal significance. There exists some works [Zhao *et al.*, 2018b]
on finding k closest objects in game maps, called k near-
est neighbors (k NN), but most of the existing techniques are
not designed for the dynamic game environments. Searching
for relevant nearby objects in dynamic game environments is
challenging as it requires efficiently handling real-time ob-
ject updates while maintaining fast query performance. Ad-
ditionally, in many practical applications, it is important to
find nearby objects that match a specific textual description,
e.g., finding the nearest “healing unit”. In such scenarios,
simply identifying the closest objects without considering
whether they match the required textual description is insuf-
ficient. While our focus in this paper is on game maps, there
are many applications of the problem we study in this pa-
per beyond game maps such as in indoor location-based ser-
vices [Cheema, 2018], home assistant technologies [Luria *et al.*,
2016; Umair *et al.*, 2021], automated warehouses [Custodio
and Machado, 2020], asset tracking [Krishnan and Men-
doza Santos, 2021] etc.

To the best of our knowledge, we are the first to study such
textual object search in dynamic game environments. Specif-
ically, we study keyword k NN queries that find the k closest
objects that satisfy the query keywords. The state-of-the-art
algorithms for traditional k NN queries are: Incremental Eu-
clidean Restriction(IER)-Polyanya [Zhao *et al.*, 2018a]; and
Interval Heuristic (IH) [Zhao *et al.*, 2018b]. Although both
IER-Polyanya and IH can be extended to answer keyword
 k NN queries (see Section 3.2), they either suffer from poor
query performance or inefficient update handling. Specifi-
cally, IER-Polyanya utilises R-tree for efficient object search
but suffers from poor update handling because R-tree is not
well-suited for dynamic environments. In contrast, IH em-
ploys navigation mesh which can be efficiently updated but
suffers from poor query performance especially when the re-
sult objects are not close to the query.

Given the limitations of IER-Polyanya and IH, there is a
need to design an effective index that can be efficiently up-
dated in highly dynamic environments such as game maps
and, at the same time, allows efficient query processing. To

86 this end, we present a simple lightweight index, called Grid
87 Tree, which cannot only efficiently handle object updates but
88 also allows efficiently processing keyword k NN queries and
89 several variants. We evaluate our approach using widely used
90 game benchmarks [Sturtevant, 2012] and realistic keyword
91 datasets for these games. We compare our approach with
92 IER-Polyanya, IH, and IER-EHL (a faster version of IER-
93 Polyanya), and show that our approach achieves the best of
94 both worlds. Specifically, it can handle object updates by
95 up to 2 orders of magnitude faster than IER-Polyanya and
96 IER-EHL, and its update cost is comparable to IH (specifi-
97 cally, faster for object movements and slower for object in-
98 sertions/deletions). At the same time, its query performance
99 is comparable to IER-EHL, several times faster than IER-
100 Polyanya, and up to two orders of magnitude faster than IH.
101 We also discuss how our approach can efficiently answer sev-
102 eral other variants of textual object search queries.

103 2 Preliminaries

104 We consider a Euclidean plane containing a set of obstacles,
105 each represented as a polygon. Two points in the plane are
106 **visible** to each other (i.e., **co-visible**) iff there exists a straight
107 line connecting them that does not pass through any obsta-
108 cle. A **path** \mathcal{P} between two points x and y is an ordered set
109 of points $\langle p_1, p_2, \dots, p_n \rangle$ where $p_1 = x, p_n = y$ and every
110 successive pair of points p_i and p_{i+1} ($i < n$) is co-visible.
111 The **length** of a path \mathcal{P} is the cumulative Euclidean distance
112 between the successive pairs of points, denoted as $|\mathcal{P}|$, i.e.,
113 $|\mathcal{P}| = \sum_{i=1}^{n-1} Edist(p_i, p_{i+1})$ where $Edist(p_i, p_{i+1})$ is the
114 Euclidean distance between p_i and p_{i+1} . A path \mathcal{P} is a **short-**
115 **est path**, denoted as $sp(x, y)$, if there is no other path between
116 x and y shorter than \mathcal{P} . We use $d(x, y)$ to denote the length
117 of the shortest path, i.e., $d(x, y) = |sp(x, y)|$.

118 We consider a set of objects O in the traversable (i.e.,
119 non-obstacle) area of the Euclidean plane. Each object
120 $o_i \in O$ is represented as a tuple $(o_i.\rho, o_i.\tau)$ where $o_i.\rho$
121 is a two-dimensional point representing location of o_i in
122 the Euclidean plane and $o_i.\tau$ is its textual description rep-
123 resented as a set of keywords. Similar to many existing
124 works in dynamic environments [Mouratidis *et al.*, 2005;
125 Hidayat *et al.*, 2022], we consider a timestamp model where
126 the time domain is discretised into a set of timestamps T . The
127 set of objects O may change between two consecutive times-
128 tamps if new objects are added to O or some existing objects
129 are deleted. We use O^t to denote the set of objects at a times-
130 tamp $t \in T$. Similarly, location and/or textual description
131 of an object o_i may change and we use $o_i^t = (o_i^t.\rho, o_i^t.\tau)$
132 to represent an object $o_i^t \in O^t$ at a timestamp $t \in T$.

133 A query q is also a tuple $(q.\rho, q.\tau)$ representing its loca-
134 tion and query keywords. There are many variants of textual
135 object search but, in this work, our main focus is on boolean
136 k NN query [Chen *et al.*, 2013] which is one of the most pop-
137 ular keyword queries.

138 **Definition 1. boolean k NN Query:** Given a query $q =$
139 $(q.\rho, q.\tau)$ issued at timestamp t and the set of objects O^t , find
140 up to k objects closest from the query location $q.\rho$ among
141 the objects that contain all query keywords $q.\tau$. Formally,
142 the result set of the query R contains up to k objects from

O^t such that $\forall o_i^t \in R: q.\tau \subseteq o_i^t.\tau$ and $\nexists o_j^t \in O^t \setminus R:$ 143
 $d(q.\rho, o_j^t.\rho) < d(q.\rho, o_i^t.\rho) \wedge q.\tau \subseteq o_j^t.\tau.$ 144

Example 1. Figure 1 shows a game map where black poly- 145
gons represent obstacles (i.e., non-traversable area). The 146
maps contains six objects o_1 to o_6 along with their associated 147
textual description, e.g., $o_1.\tau = \{w, x\}$. Consider a boolean 148
1NN query q shown on the map with $q.\tau = \{x, y\}$. The ob- 149
jects o_2, o_3 and o_6 are the candidate objects (shown in green 150
filled circles) as each of these contains both of the query key- 151
words x and y . However, o_2 is the closest object among these 152
from q considering the obstacle-avoiding distance. Thus, the 153
result for query q is o_2 . 154

In Section 4.4, we discuss how our approach can be used 155
to answer several variants of this query. Also, note that a 156
traditional k NN query is a special case of boolean keyword 157
 k NN query when there is no query keyword, i.e., $q.\tau = \emptyset$. 158

159 3 Related Work

160 3.1 Pathfinding in Game Maps

161 Pathfinding in game maps, finding shortest path between two
162 locations, has been extensively studied, e.g., see [Demyen
163 and Buro, 2006; Oh and Leong, 2017; Uras and Koenig,
164 2015; Shen *et al.*, 2022] and references therein. Next, we
165 briefly discuss two state-of-the-art algorithms most relevant
166 to this work.

Polyanya [Cui *et al.*, 2017] is an efficient online pathfinding
167 algorithm. The algorithm employs a navigation mesh [Kall-
168 mann and Kapadia, 2014] which divides the traversable area
169 into a set of convex polygons. Polyanya instantiates a search
170 similar to A* algorithm and treats polygon edges of the navi-
171 gation mesh as search nodes. It iteratively expands the edges
172 according to heuristic values considering their distances from
173 source and target. When the search accesses the polygon con-
174 taining target, the target is also added in the queue as a search
175 node. The algorithm terminates when the target is expanded. 176

Euclidean Hub Labeling (EHL) [Du *et al.*, 2023] is the
177 state-of-the-art pathfinding algorithm. It employs hub label-
178 ing [Abraham *et al.*, 2011] which is a highly efficient ap-
179 proach to compute shortest paths/distances in graphs. In the
180 preprocessing phase, EHL computes hub labels on the visi-
181 bility graph containing the convex vertices of the map. A
182 uniform grid is superimposed on the map and, for each cell c
183 of the grid, hub labels of the vertices visible from c are copied
184 to the cell c . During query processing, the hub labels of the
185 cells containing source and target are combined to find the
186 common hub nodes and compute the shortest path/distance. 187

188 3.2 Object Search in Game Maps

189 Object search on geo-textual data has been very well-
190 studied [De Felipe *et al.*, 2008; Cong *et al.*, 2009; Chen *et al.*,
191 2013; Chen *et al.*, 2020; Xu *et al.*, 2022] due to its applica-
192 tions in map-based services. Unfortunately, these techniques
193 are not suitable for game maps which are highly dynamic and
194 are represented differently, as a Euclidean plane containing
195 polygonal obstacles. Next, we briefly discuss two best-known
196 algorithms for computing traditional k NN queries in game
197 maps and their extension for textual object search. 197

198 **Interval Heuristic (IH)** [Zhao *et al.*, 2018b] is based on
 199 Polyanya and replaces the heuristic of the A* search such
 200 that the search incrementally explores the space like Dijkstra
 201 search. When the search reaches a polygon that contains an
 202 object, the object is also added to the queue. The algorithm
 203 terminates when k objects are expanded. IH can be easily
 204 extended to answer keyword k NN queries by pruning every
 205 accessed object that does not satisfy query keywords. Since
 206 IH employs Polyanya which exploits a navigation mesh, hand-
 207 ling object updates is quite efficient. Specifically, IH re-
 208 quires maintaining the objects located in each polygon of the
 209 navigation mesh. Thus, if an object changes its location, the
 210 object is deleted from its previous polygon and added to its
 211 new polygon. If the object remains in the same polygon, the
 212 navigation mesh does not need any update.

213 **IER-Polyanya** [Zhao *et al.*, 2018a] employs an R*-
 214 tree [Beckmann *et al.*, 1990] and incrementally retrieves near-
 215 est objects to the query location according to their Euclidean
 216 distances. For each retrieved object, it calls Polyanya to com-
 217 pute its actual distance from the query. The algorithm termi-
 218 nates when the Euclidean distance of the next retrieved object
 219 is no smaller than the actual distances of k NNs. To handle
 220 keyword queries, we use IR-tree [Li *et al.*, 2010], a popular
 221 extension of R*-tree to handle spatio-textual data. While R*-
 222 tree and IR-tree allow efficient query processing, it is com-
 223 putationally expensive to update them. For example, the lo-
 224 cation update is handled by first updating the structure of IR-
 225 tree in a way similar to how R-tree handles updates. Then,
 226 the textual information associated with each node is updated
 227 accordingly. Since the nodes of R*-tree and IR-tree may need
 228 to be expanded or shrunk with the updates, they are not well-
 229 suited for highly dynamic environments such as game maps.

230 The other two approaches in [Zhao *et al.*, 2018a], Target
 231 Heuristic (TH) and Fence Heuristic (FH), are not suitable for
 232 highly dynamic environment and were outperformed by both
 233 IER-Polyanya and IH in our initial experiments and, there-
 234 fore, are not discussed/compared against in this paper.

235 4 Our Approach

236 First, we present the details of our index, called Grid Tree,
 237 in Section 4.1. Then, in Section 4.2, we discuss how the
 238 Grid Tree is updated with the changes in the underlying data.
 239 Section 4.3 presents our query processing algorithm. Finally,
 240 Section 4.4 discusses how the proposed approach can be eas-
 241 ily extended to answer a variety of other queries. Our algo-
 242 rithm relies on a shortest distance computation module which
 243 is responsible for computing $d(x, y)$ between any two points
 244 x and y . Although any shortest distance computation algo-
 245 rithm can be used for this purpose, we employ Euclidean Hub
 246 Labeling (EHL) [Du *et al.*, 2023] because it is the most effi-
 247 cient shortest distance computation algorithm. We intention-
 248 ally keep our index separate from the shortest distance com-
 249 putation module because it offers flexibility in system design.

250 4.1 Grid Tree

251 **Motivation.** Traditional indexes such as R-tree [Guttman,
 252 1984], R*-tree [Beckmann *et al.*, 1990], kd-tree [Ooi, 1987],
 253 and Quad-tree [Smith and Chang, 1994] as well as their ex-

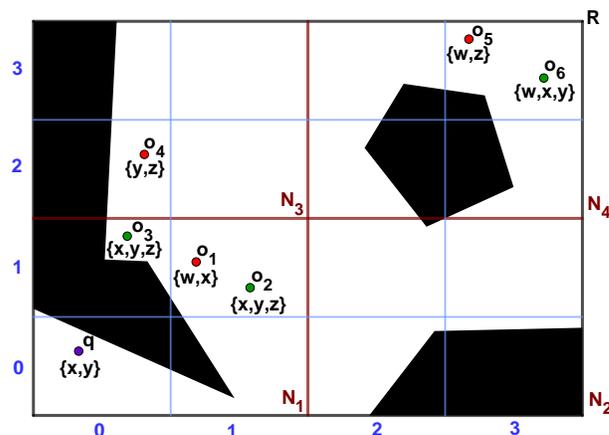


Figure 1: Boolean keyword k NN query: o_2 is the INN.

254 tensions [Chen *et al.*, 2013] to index textual information, al-
 255 low efficient query processing for a variety of queries. How-
 256 ever, a major limitation of these indexes is that they are not
 257 suitable for dynamic environments such as game maps where
 258 object updates are frequent. Therefore, we need an index
 259 that can be efficiently updated in the dynamic environment
 260 and allows efficient query processing. Next, we present the
 261 details of a simple, easy-to-implement and effective index,
 262 called Grid Tree, that can be efficiently updated and allows
 263 efficient query processing.

264 **Structure of Grid Tree.** Root node of the Grid Tree is a min-
 265 imum bounding rectangle (MBR) of the whole map. Each
 266 node is recursively divided into four equal sized children
 267 until the size of each child node is smaller than a threshold (to
 268 be discussed in experiments). Consider a Grid Tree of height
 269 h where the root node is at level 0 and the leaf nodes are at
 270 level h . There are $2^i \times 2^i$ equal-sized nodes at level i of the
 271 Grid Tree. The leaf nodes constitute a uniform grid contain-
 272 ing $2^h \times 2^h$ equal-sized cells. Hereafter, we use the terms leaf
 273 nodes and cells interchangeably to refer to the level h nodes.

274 For each leaf node n , we store an object list containing the
 275 IDs of the objects that are located inside n . Additionally, for
 276 every node n in the Grid Tree, we store a keyword list. Here-
 277 after, when we say “objects inside a node n ”, we refer to all
 278 the objects that are in the subtree rooted at the node n . The
 279 keyword list of the node n contains all unique keywords of
 280 the objects inside n along with the frequency of each key-
 281 word, e.g., if a keyword κ appears in 5 objects inside n , its
 282 frequency is 5. We implement the keyword list as a hash map
 283 so that frequency of any keyword can be obtained/updated ef-
 284 ficiently. Note that object lists are stored only for leaf nodes
 285 whereas keyword lists are stored for all nodes of the tree.

286 **Example 2.** Figures 1 and 2 show a Grid Tree of height 2.
 287 The root node R of the Grid Tree is the MBR covering the
 288 whole space. The root node has four equal-sized children N_1
 289 to N_4 shown in solid red lines. Each of these nodes is further
 290 subdivided into four children. The leaf nodes at level 2 repre-
 291 sent a 4×4 grid (see cells shown in blue lines). In Figure 1,
 292 we refer to each leaf node as $C_{i,j}$ where i and j correspond to
 293 its position along x -axis and y -axis, respectively (see the blue

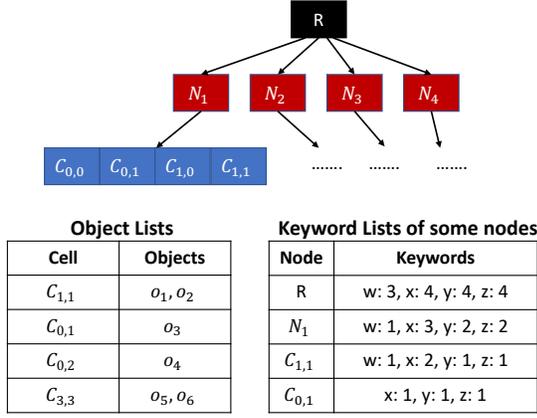


Figure 2: Grid Tree: Children of N_2 to N_4 are not shown. Object Lists and Keyword Lists of **some** of the nodes are shown.

same leaf node, we do not need to update anything. Otherwise, we delete the object from the object list of n and add it to the object list of n' . Keyword lists of n and n' are also updated accordingly, i.e., by decrementing the frequency of each keyword $\kappa \in o_i^t$ in the keyword list of n and incrementing it by one in the keyword list of n' . Then, the parent nodes of n and n' are iteratively accessed and their keyword lists are updated accordingly until a common ancestor of n and n' is reached. Note that the keyword list of the common ancestor does not need to be updated.

Example 3. Consider the example shown in Figures 1 and 2 and assume that the object o_3 moves from its current cell $C_{0,1}$ to the cell $C_{1,1}$. We delete o_3 from the object list of $C_{0,1}$ and add it to the object list of $C_{1,1}$. The keyword list of $C_{0,1}$ is updated by decrementing the frequency of each of the keywords x, y and z by one and, consequently, the keyword list of $C_{0,1}$ becomes empty. Then, the keyword list of $C_{1,1}$ is updated by incrementing the frequencies of x, y and z by one each. As a result, the keyword list of $C_{1,1}$ is updated to $\{w: 1, x: 3, y: 2, z: 2\}$. Next, we access the parent nodes of the two cells $C_{0,1}$ and $C_{1,1}$. Since both have the same parent N_1 , the keyword list of N_1 does not need to be updated.

Handling textual change of an object. Assume that textual description of an object changes between two timestamps. For each deleted keyword κ (i.e., $\kappa \in o_i^{t-1} \cdot \tau \wedge \kappa \notin o_i^t \cdot \tau$), we update the keyword list of the leaf node n containing $o_i^t \cdot \rho$ by decrementing the frequency of κ by one. For each newly added keyword κ' (i.e., $\kappa' \notin o_i^{t-1} \cdot \tau \wedge \kappa' \in o_i^t \cdot \tau$), we update the keyword list of n by incrementing the frequency of κ' by one. Keyword lists of all ancestors of n are also updated.

If both the location and the textual description of an object change between two timestamps, we delete the object o_i^{t-1} and insert o_i^t as discussed earlier.

Complexity Analysis. Here, we provide complexity analysis for handling the updates mentioned above. A key operation for handling the updates is to identify the leaf node of the Grid Tree that contains a particular location. This can be done in $O(1)$ because the leaf nodes correspond to a grid of $2^h \times 2^h$ equal-sized cells where h is the height of the tree. The object insertion and deletion in the object list of a cell can also be done in $O(1)$. Specifically, the object list of each cell is implemented as a linked list. Furthermore, we maintain a global object array containing all objects indexed by their IDs. For each object o_i^t , this array stores a pointer to the place of o_i^t in the object list of the cell containing it. This allows deleting an object from the object list in $O(1)$. A new object is always inserted at the end of the object list and its place in this object list is reflected in the global object array. Keyword lists are implemented as hash tables. Although the worst-case complexity is linear to the number of keywords, on average, the cost is $O(1)$. Consider an update involving \mathcal{K} keywords, the average cost of updating the keyword list is $O(\mathcal{K})$. For all of the updates mentioned above, we need to update at most $O(h)$ nodes. Therefore, the total cost for each update operation is $O(\mathcal{K}h)$ on average.

We remark that while the cost of handling location change of an object is $O(\mathcal{K}h)$ in general, the cost when the object moves within the same leaf node is $O(1)$. This is because, in

numbers outside the map), e.g., q is located in the cell/leaf node $C_{0,0}$ and o_4 is located in the leaf node $C_{0,2}$. Figure 2 shows the structure of Grid Tree as well as the object lists and keyword lists for some of the nodes. Since the leaf node $C_{1,1}$ contains o_1 and o_2 , its object list consists of o_1 and o_2 . Keyword list of $C_{1,1}$ contains all keywords present in o_1 and o_2 along with their frequencies, e.g., each of w, y and z appears in only one object whereas x appears in both o_1 and o_2 . The keyword list of N_1 represents the keywords and their frequencies for all objects in N_1 (i.e., o_1, o_2 and o_3). The keyword list of the root represents keywords and frequencies of all six objects. For simplicity, Figure 2 shows object lists and keyword lists only for **some** cells and nodes of the tree.

4.2 Updating Grid Tree

Now, we explain how the Grid Tree is updated at a timestamp $t \in T$. Although our focus in this paper is on handling moving objects, for completeness, we discuss how to insert an object, delete an object, and handle the change in the location/text of an object.

Inserting a new object. To insert a new object o_i^t , we first identify the leaf node n that contains the location $o_i^t \cdot \rho$. Then, o_i^t is added to the object list of n . Keyword list of n is also updated by incrementing the frequency of each keyword $\kappa \in o_i^t \cdot \tau$ by one. If a keyword does not exist in the keyword list, it is added with frequency one. Then, all the ancestor nodes of n are iteratively accessed and their keyword lists are updated in the same way.

Deleting an object. To delete an object o_i^t , it is deleted from the object list of the node n containing it. The keyword list of n is also updated by decrementing the frequency of each keyword $\kappa \in o_i^t \cdot \tau$ by one. If the frequency of any keyword is reduced to zero, it is deleted from the keyword list. The keyword lists of all ancestor nodes of n are also updated in the same way.

Handling the location change of an object. Assume that the location of an object changes between two timestamps, e.g., $o_i^{t-1} \cdot \rho \neq o_i^t \cdot \rho$. We update the Grid Tree at timestamp t as follows. We identify the leaf nodes n and n' that contain the locations $o_i^{t-1} \cdot \rho$ and $o_i^t \cdot \rho$, respectively. If n and n' are the

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Algorithm 1: Boolean k NN query processing

Input: q, ρ, q, τ, k : query location, query keywords and k
Output: R : query results

```
1  $R = \phi; d^k = \infty;$ 
2 Initialise a min-heap  $H$  with the root node of Grid Tree ;
3 while  $H \neq \phi$  do
4   deheap an entry  $e$  from  $H$  ;
5   if  $e.key \geq d^k$  then
6     return  $R$ ;
7   if  $e$  is an object then
8     compute  $d(q, \rho, e, \rho)$ ;
9     if  $d(q, \rho, e, \rho) < d^k$  then
10      update  $R$  and  $d^k$  by object  $e$ ;
11   else if  $e$  is a leaf node then
12     for each object  $o_i^t$  in the object list of  $e$  do
13       if  $q, \tau \subseteq o_i^t, \tau$  then
14         insert  $o_i^t$  in  $H$  with key
15            $mindist(q, \rho, o_i^t, \rho)$ ;
16   else
17     for each child node  $c$  of  $e$  do
18       if  $c$  contains all query keywords  $q, \tau$  then
19         insert  $c$  in  $H$  with key  $mindist(q, \rho, c)$ ;
19 return  $R$ ;
```

391 this case, we do not need to update the object list and keyword
392 list of any node. This enables our proposed index to handle
393 moving objects very efficiently. Traditional indexes such as
394 R-tree, Quad-tree and kd-tree cannot handle moving objects
395 in $O(1)$.

396 4.3 Query Processing

397 Algorithm 1 shows the details of our algorithm to compute
398 boolean k NNs of a query using the Grid Tree. The algo-
399 rithm initialises the result set R to be empty and d^k to infinity
400 (line 1) where d^k is the distance of the k^{th} closest object in
401 R . A min-heap H is initialised by inserting the root node of
402 the Grid Tree (line 2) with key set to zero. The key of an entry
403 e (denoted as $e.key$) inserted in the heap is a lower bound
404 distance from q, ρ to the entry e (e.g., minimum Euclidean dis-
405 tance from q, ρ to the node e). In each iteration, the algorithm
406 de-heaps an entry e from the heap. If $e.key$ is at least equal
407 to d^k , the algorithm terminates by returning the result set R
408 (line 6). This is because all remaining entries have distances
409 from the query at least equal to d^k and, therefore, cannot con-
410 tain an object closer to the query than the k^{th} closest object.

411 If the de-heaped entry e is an object, its distance from
412 the query $d(q, \rho, e, \rho)$ is computed (line 8). This distance
413 can be computed using any of the existing pathfinding algo-
414 rithms. In our implementation, we use Euclidean Hub La-
415 beling (EHL) [Du *et al.*, 2023] which is the state-of-the-art
416 shortest path computation algorithm in game maps. If this
417 distance is smaller than d^k , the result set R and d^k are up-
418 dated accordingly (line 10). Specifically, we implement R
419 as a max-heap with keys set to distances between the query
420 and the objects stored in R . We insert e in R and ensure that
421 R contains at most k objects after each iteration. If after in-
422 serting e , R contains more than k objects, the object with the
423 largest distance (i.e., the top entry in the max-heap) is deleted

from R . If R contains less than k objects, d^k is kept to be
infinity. Otherwise, d^k is set to the distance of the k^{th} closest
object in R (i.e., the key of the top entry in the max-heap).

If the de-heaped entry e is a leaf node of the Grid Tree, we
process the objects in its object list (line 12) and insert each
object o_i^t that contains all query keywords in the min-heap H
(lines 13 and 14). The key of each object inserted in the min-
heap is a lower bound distance between the query and the
object locations. In our implementation, we use Euclidean
distance between q, ρ and o_i^t, ρ as the lower bound distance.

Finally, if e is a non-leaf node of the Grid Tree, we process
each child node c of e as follows. First, we check if c contains
all query keywords or not (line 17). Specifically, a node c
contains all query keywords q, τ iff, for every keyword $\kappa \in$
 q, τ , κ exists in the keyword list of c . If c contains all query
keywords, it is inserted in the min-heap with key set to a lower
bound distance (e.g., minimum Euclidean distance) between
the query location and the node c . If the heap H becomes
empty, the algorithm returns R (line 19) which contains up to
 k closest objects found by the algorithm.

Remarks. Although our implementation uses minimum Eu-
clidean distance as the lower bound at lines 14 and 18, other
lower bounds can also be used. One feature of the Grid Tree is
that its nodes do not spatially change regardless of the updates
(unlike other popular spatial indexes such as R-tree, kd-tree
etc.). Therefore, it is possible to precompute and store lower
bound distances. E.g., one may precompute minimum dis-
tances from the convex vertices in the map to all nodes of the
Grid Tree. During query processing, the closest visible vertex
from the query can be used to obtain a lower bound distance
for any node of the Grid Tree by using triangular inequality.

445 4.4 Extensions

Generalisation of boolean k NN query. Boolean k NN
queries can be generalised to find k closest objects that con-
tain at least n keywords in q, τ , e.g., for each result object
 $o_i^t \in R, |q, \tau \cap o_i^t, \tau| \geq n$ where $|X|$ denotes the number of ele-
ments in a set. This generalised version can be easily handled
by changing the conditions at lines 13 and 17 accordingly.

Top- k spatial keyword query. In top- k spatial keyword
query [Chen *et al.*, 2013], each object is assigned a *score*
computed using a scoring function that considers both its tex-
tual similarity to the query keywords and distance from query
location. The query requires finding k objects with the small-
est scores (assuming lower scores are better). Our algorithm
can answer such queries as follows. The min-heap H is mod-
ified such that the keys are minimum scores of the entries
instead of minimum distances. The minimum score of an en-
try e (an object or a node) is computed using the minimum
Euclidean distance between e and query location and the best
possible textual similarity of e to query keywords consider-
ing the keyword list of e . The algorithm employs s^k , score of
the k^{th} object in R , instead of d^k . The conditions at lines 13
and 17 of the algorithm are modified such that an entry is
inserted in H only if its minimum score is smaller than s^k .

Keyword range query. Given a distance range r , a keyword
range query returns every object $o_i^t \in O^t$ that satisfies the
query keywords and $d(q, \rho, o_i^t, \rho) < r$. Our algorithm can be

Game	#Maps	# Cells	# Trav. Cells	# Vertices
DA	67	151,420	15,911	1182.9
DAO	156	134,258	21,322	1727.6
BG	75	262,144	73,930	1294.4
SC	75	446,737	263,782	11487.5

Table 1: Total number of maps, and average number of total cells, traversable cells and vertices in each benchmark.

easily modified by replacing d^k with r . This ensures that all objects with distances less than r are included in R .

Constrained keyword k NN queries. In constrained keyword k NN queries, the goal is to find the k closest objects that satisfy the query keywords and lie in a specified region (called constrained region) of the map. E.g., one may want to find the nearest “artillery unit” in a specific zone of the game map. This query can be answered easily using our proposed algorithm by adding a filter to prune every entry e that does not overlap with the constrained region.

5 Experiments

5.1 Settings

We run our experiments on a 3.2 GHz Intel Core i7 machine with 32 GB of RAM. All the algorithms are implemented in C++ and compiled with -O3 flag. We run experiments on widely used game map benchmarks [Sturtevant, 2012] of four popular games: Dragon Age II (DA); Dragon Age Origins (DAO); Baldur’s Gate II (BG) and StarCraft (SC). In total, this gives us 373 maps each represented as a grid map. Table 1 shows details of these benchmarks including the average size – represented by total number of cells and the total number of traversable (i.e., non-obstacle) cells in the maps – and average number of obstacle vertices. We generate the objects, their keywords and queries as follows.

Object generation. Initial location of each object is a randomly generated point in the traversable region of the map. We evaluate the effect of object density which is the ratio of number of objects to the number of traversable cells in the map, e.g., object density of 1% indicates that the number of objects is 1% of the total number of traversable cells in the map. We vary the density from 0.1% to 10% and the default density is 1%. Although we also study the effect of insertions/deletions, our main focus is on moving objects. We define *mobility* of an object set as the percentage of objects that move between two timestamps. We vary the mobility from 10% to 100% and the default mobility is 70%. We generate the moving objects as follow. For each moving object, we randomly choose a target location in the traversable region of the map and compute the shortest path from the initial location of the object to the target location. The object then starts moving towards the target and travels 1 unit distance (i.e., which is equal to the width/height of one cell in the map) in each timestamp. When an object reaches the target, a new randomly generated target is chosen and the object continues to travel on the shortest path towards this new target.

Keyword generation. For each game, we use ChatGPT (Jan 9 version) to obtain 100 items in the game along with their descriptions. Specifically, we use prompts like “de-

scribe characters in [game map]” to get a list of items including characters, units, weapons, gems, potions etc. We keep prompting ChatGPT until it generates 100 items and their descriptions¹. We use `nltk`, an NLP library, to remove stop words and normalise the remaining words (e.g., “abilities” and “ability” both are normalised to “ability”). After this pre-processing, maximum, minimum, and average number of keywords per item in each game are as follows: DA (19,7,15); DAO (17,7,12); BG (17,6,12); SC (18,7,11). For each object, we randomly assign it to an item type in the relevant game. Let m be the number of keywords in that item, we randomly choose a number r between 1 and m and randomly assign r keywords of this item to the object.

Query generation. For each experiment, we generate 100 queries per timestamp. Location of each query is randomly generated in the traversable region of the map. We evaluate the effect of k which is varied from 1 to 10 where the default value of k is 3. We also evaluate the effect of number of query keywords by varying the number of query keywords from 0 to 3 where the default number of keywords is 2. Following the existing works on geo-textual object search [Chen *et al.*, 2013], we generate a query containing x keywords by randomly choosing an object from the map and selecting x words at random from the object as the query keywords. This ensures that the combination of query keywords is meaningful and at least one object satisfies the query keywords.

Algorithms evaluated. Our approach, Grid Tree, is shown as GT in the experiments. We evaluate different sizes of Grid Tree each shown as $GT(m)$ where $GT(m)$ is the Grid Tree with each leaf node of size at most $m \times m$ units. E.g., in $GT(4)$, we stop recursively dividing nodes into children when the node size becomes less than 4×4 .

We compare our approach with two state-of-the-art approaches presented in [Zhao *et al.*, 2018a]: IER-Polyanya (shown as **IER-Pol**) and Interval Heuristic (**IH**). We use the source code provided by the authors. We also compare against **IER-EHL** which is the same as IER-Pol except that the shortest distances are computed using EHL [Du *et al.*, 2023] instead of Polyanya [Cui *et al.*, 2017]. This gives a like-for-like comparison with our approach as we also employ EHL for shortest distance computation.

5.2 Results

Each experiment is run for 50 timestamps and, for each timestamp t , we first update the underlying index considering all object updates at t and then process 100 queries on the updated index. We report average update time per timestamp for all 50 timestamps as well as the average query processing time for all 5000 queries.

Effect of object density: Figure 3 shows the effect of object density on query time (top row) and update cost (bottom row) on each of the four benchmarks. Overall, the fastest algorithms in terms of query processing are $GT(16)$ and $GT(64)$ whereas the best performing algorithms in terms of handling updates is $GT(64)$. We discuss the details of query time and update time below.

¹<https://github.com/goldi1027/GT-EHL>

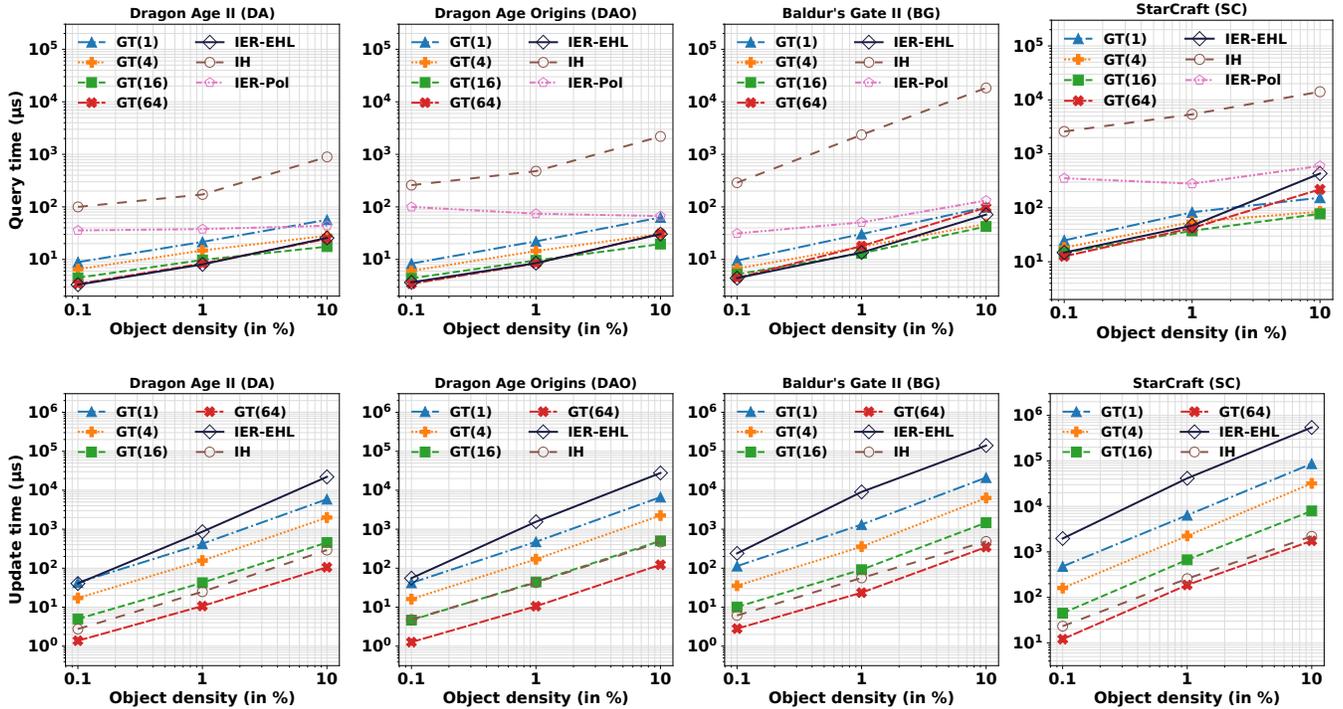


Figure 3: Effect of object density on query time (top row) and update time (bottom row) for each approach on default settings ($k = 3$, mobility = 70%, # of query keywords = 2).

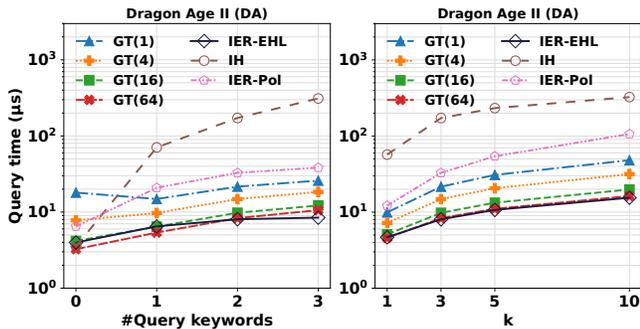


Figure 4: Effect of # of query keywords and k on query time

584 *Query time.* For lower object density, query performance
 585 of our approach improves when the leaf nodes are bigger
 586 (e.g., GT(64)) because the tree height is smaller and the
 587 search needs to traverse fewer nodes. However, as the den-
 588 sity increases, the performance of GT(64) degrades because
 589 each leaf node contains more object requiring the algorithm to
 590 process a larger number of objects. IER-EHL outperforms the
 591 other competitors IH and IER-Poly, however, its performance
 592 is comparable to GT(16) and GT(64) for lower object density
 593 but worse for higher object density, e.g., for the SC bench-
 594 mark, the query time of IER-EHL is several times higher than
 595 that of GT(16). IH is the slowest algorithm (often more than
 596 2 orders of magnitude slower than our algorithms) because
 597 it needs to incrementally explore a large search space before
 598 it can find the answers. IER-Poly is slower than IER-EHL

599 mainly because Polyanya is slower than EHL. However, the
 600 performance of IER-Poly does not necessarily degrade with
 601 the increase in object density. This is because the cost of
 602 shortest distance computation for Polyanya decreases when
 603 the objects are closer to the query and, for higher density, the
 604 result objects are found closer to the query.

605 *Update time.* The update handling time of Grid Tree signif-
 606 icantly improves as the size of leaf nodes increases, e.g., see
 607 GT(64). This is because the height of the tree is smaller for
 608 GT(64) which means fewer nodes are needed to be updated.
 609 Also, the moving objects leave the leaf nodes less often be-
 610 cause the leaf nodes are bigger as compared to the leaf nodes
 611 in GT(1). The update handling time of GT(64) is up to 2 or-
 612 ders of magnitude lower than the IER-EHL because IR-tree
 613 is unable to efficiently handle moving objects. Note that we
 614 do not show IER-Poly because it also employs IR-tree and,
 615 therefore, its update cost is the same as IER-EHL. IH has a
 616 significantly smaller update handling time than IER-EHL be-
 617 cause it basically needs to maintain the object information in
 618 relevant polygons of the navigation mesh. However, its up-
 619 date handling time is higher than that of GT(64) but better or
 620 comparable to that of GT(16).

621 *Effect of query keywords and k .* Figure 4 shows the ef-
 622 fect of number of query keywords and k on the query perfor-
 623 mance (the update time is not affected by them). We show
 624 the results for the DA benchmark and the results for the other
 625 benchmarks follow similar trends. The query cost of all ap-
 626 proaches increases with the increase in number of query key-
 627 words. The cost of IH is most significantly affected which is
 628 mainly because, as the number of query keywords increases,

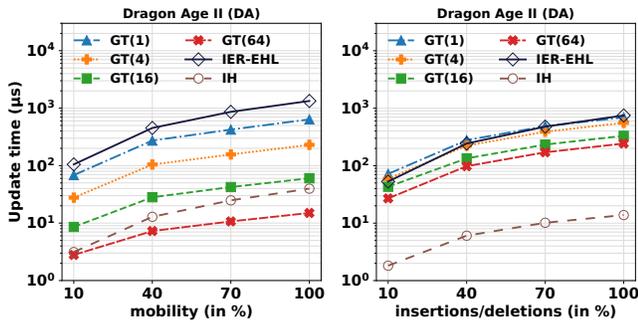


Figure 5: Update time for varying mobility and insertions/deletions.

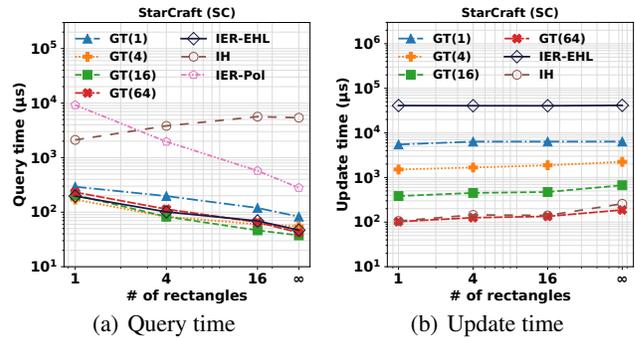


Figure 6: Effect of # of rectangles

629 there are fewer objects that contain all query keywords. As a
 630 result, IH needs to incrementally explore larger search space
 631 to find the answer. As expected, the cost of all approaches in-
 632 creases with the value of k because the search space increases.
 633 GT(64) and IER-EHL are the best performing algorithms in
 634 terms of query cost.

635 **Effect of mobility and updates.** Figure 5(left) shows the ef-
 636 fect of number of moving objects at each timestamp (shown
 637 as mobility). GT(64) handles the updates most efficiently
 638 and scales better mainly because the moving objects are less
 639 likely to leave the leaf nodes as the leaf nodes get bigger and,
 640 therefore, requiring fewer updates. Although less common in
 641 game maps than moving objects, the objects may be inserted
 642 and deleted in game maps. Figure 5(right) studies the effect
 643 of insertions/deletions in the game maps. For each experi-
 644 ment shown as $x\%$ insertions/deletions, at each timestamp t ,
 645 we first randomly insert $\frac{x}{2}\%$ of the total objects in the map
 646 as new objects and then randomly delete the same number of
 647 objects. The cost is average update cost per timestamp. The
 648 cost of our approach increases mainly because the Grid Tree
 649 needs to be traversed for each insertion and deletion (unlike
 650 object movements which may not require any update if the
 651 object is in the same leaf node). On the other hand, the cost
 652 of IH and IER-EHL is lower for insertions/deletions than for
 653 object movement. This is because to handle a single object
 654 movement, these approaches require almost double the work,
 655 i.e., deleting the object followed by reinsertion. Grid Tree
 656 can still handle updates much faster than IER-EHL but its update
 657 cost is up to 1 order of magnitude higher than IH. However,
 658 as shown earlier, IH is up to 2 orders of magnitude slower
 659 than Grid Tree thus the higher update cost pays off in terms
 660 of querying performance especially when the number of dele-
 661 tions/insertions are small compared to the number of queries.

662 **Effect of object distribution.** The previous experiments
 663 show the results where the object source and target locations
 664 are randomly distributed in the traversable space of game
 665 maps. In this experiment, we show the results for cases where
 666 object source and target locations are clustered in certain ar-
 667 eas of the map. Specifically, for each experiment, we ran-
 668 domly generate x rectangles in the traversable space where
 669 each rectangle area is 1% of the total space. Object source
 670 and target locations are then generated only within these rect-
 671 angles. We study the effect of x (i.e., the number of rect-
 672 angles/clusters) by varying x to 1, 4, 16 and infinity. Here, a

673 smaller x implies that objects are clustered in fewer regions in
 674 the map and $x = \infty$ corresponds to the random distribution.
 675 Note that the total number of objects remain the same for all
 676 experiments (set to default density of 1% as explained in Sec-
 677 tion 5.1). The query set is exactly the same as the previous
 678 experiments.

679 Figure 6(a) shows the effect of object distribution on query
 680 performance on the SC benchmark. Query times of all algo-
 681 rithms except IH increase for smaller x . This is because
 682 these algorithms use Grid Tree or IR-tree for indexing the ob-
 683 jects and the processing cost increases when the objects are
 684 densely populated in certain areas. Since IH incrementally
 685 explores the search space, its cost depends on how far the ob-
 686 jects are located from the query location. When the objects
 687 are clustered in certain areas, for most of the queries in this
 688 experiment, they are found closer which results in improved
 689 querying cost. Overall, query performance trend is similar to
 690 the previous experiments, i.e., GT is similar to or better than
 691 IER-EHL and 1 to 2 orders of magnitude faster than IH. Fig-
 692 ure 6(b) shows the effect of object distribution on the update
 693 time of the underlying indexes. The update cost of Grid Tree
 694 and IH decreases slightly for smaller x . This is because when
 695 x is small, the object source and target locations are closer
 696 to each other resulting in fewer objects moving out of the leaf
 697 nodes of the Grid Tree or the polygons of navigation mesh
 698 used in IH thus resulting in lower update cost.

699 6 Conclusions

700 This paper presents the Grid Tree, a lightweight index for
 701 storing moving objects and efficiently retrieving textually rel-
 702 evant nearby objects in dynamic video game environments.
 703 Extensive experiments on widely used game map benchmarks
 704 using realistic keywords demonstrate that the proposed ap-
 705 proach generally outperforms the state-of-the-art algorithms
 706 in terms of update time and query performance. Grid Tree
 707 is a simple, easy-to-implement and highly efficient index
 708 which makes it well-suited for deployment in video games,
 709 enabling efficient object search in highly dynamic environ-
 710 ments. This work also has applications in domains such as
 711 indoor location-based services and automated warehouses.

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